

# Leveraging Residence Time Distribution (RTD) Models to Understand Ingredient and Process Impacts in Continuous Manufacturing

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# Disclaimer



- This presentation reflects the views of the authors and should not be construed to represent FDA's views or policies.

# Process Dynamics



- The dynamics of how materials or disturbances flow through the process is a critical aspect of **process understanding**
  - Identify typical failure modes or deviations (long term vs. short term; e.g., feeder variability)
  - Evaluate response to set point changes (e.g., change in line rates)
  - Assess the impact of startup and shutdown on material quality
- Material feeding variation of formulation components can translate into drug content uniformity variation
  - The amplitude and frequency of variations in the component feed rates and the capability of the process to dampen these variations must be fully understood
- Obtain an **understanding of process dynamics** by characterizing the Residence Time Distribution (RTD)
  - RTD is a probability distribution that describes the amount of time a mass or fluid element remains in a process

# Utilization of RTD in Control Strategy for CM



- **Supporting Sampling Strategy**

- Detectability of transient disturbances impacted by the relationship between process dynamics and sampling frequency

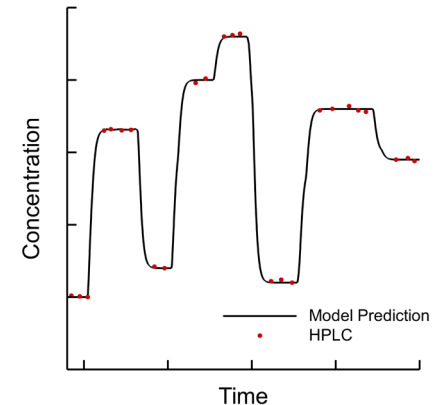
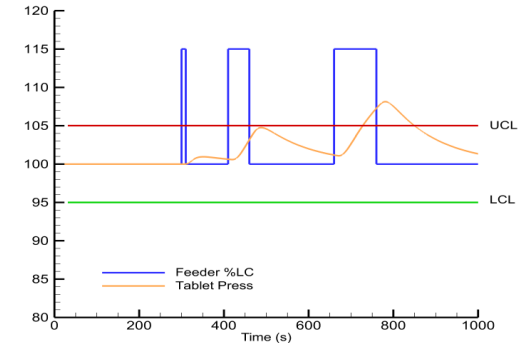
- **Material Traceability**

- Understanding of propagation of a disturbance between extraction points in the system is important to justify the amount of material at risk due to a disturbance

- **Process Monitoring**

- Predicting blend concentrations based on measured input feeding variability

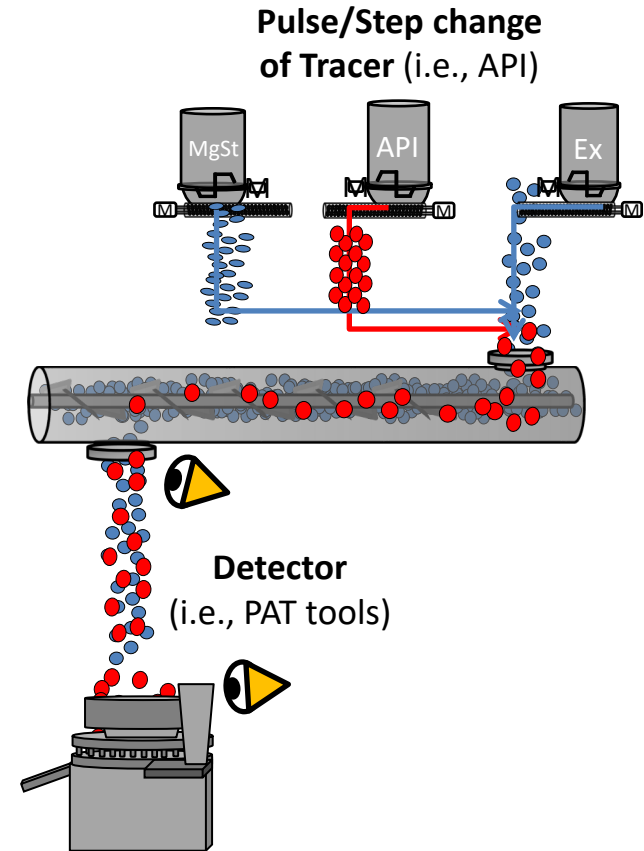
Assessment of data submitted on RTD will depend on how it is used in the control strategy



# Characterizing Continuous Processes



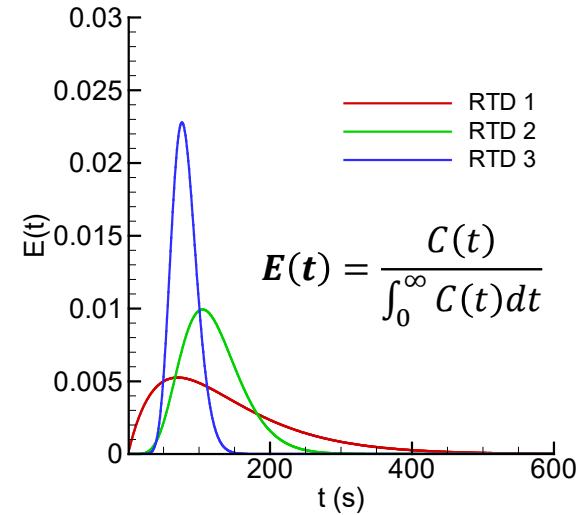
- Continuous feeders dispense material (API, excipients) into unit operations
- System is allowed to reach steady state
- Tracer material is introduced into system
  - Pulse or step change
  - API typically used as tracer
- PAT tools located downstream measure concentration of tracer exiting process as a function of time



# RTDs and Their Characterization



- A **Residence Time Distribution (RTD)** is a probability distribution that describes how long material spends in a process
  - Well-established engineering approach for non-ideal flow
- RTDs have been shown to depend on material properties, process parameters, and equipment configuration
- RTDs  $[E(t)]$  can be characterized by moments describing their shape
  - **Mean Residence Time (MRT,  $\tau$ )** is the average amount of time material spends in the system
  - **Mean Centered Variance (MCV,  $\sigma_\tau^2$ )** describes the width of the distribution (i.e., the amount of back-mixing)



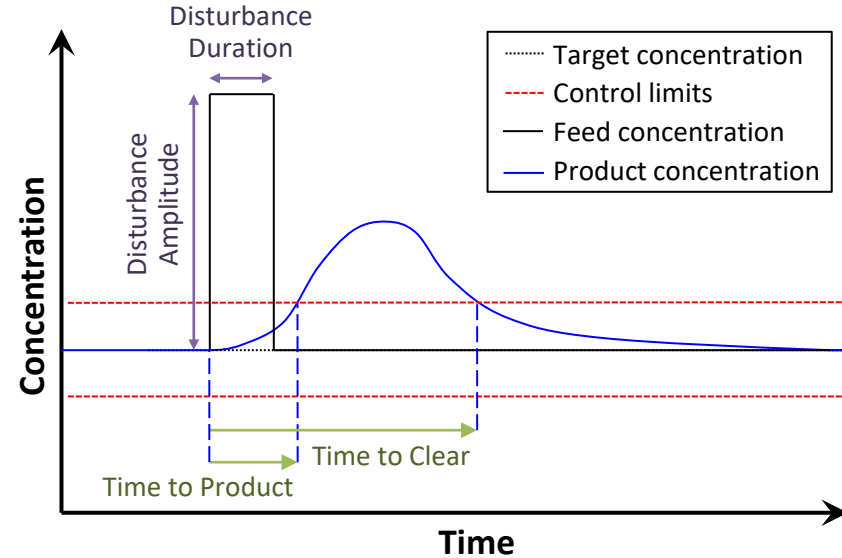
$$MRT = \tau = \int_0^\infty t \cdot E(t) dt$$

$$MCV = \sigma_\tau^2 = \int_0^\infty \frac{(t - \tau)^2}{\tau^2} E(t) dt$$

# CM Process Control Using RTDs



- Isolation and rejection of non-conforming material is a critical aspect of CM process control strategy
  - Planned process start-ups and shut-downs
  - Temporary process disturbances or upsets
- Material diversion points can be placed downstream of detectors, subjected to feed-forward control
- RTDs provide an understanding of how fast disturbances propagate and spread through a system
  - Enables real-time prediction of feeding material disturbances on blend and content uniformity

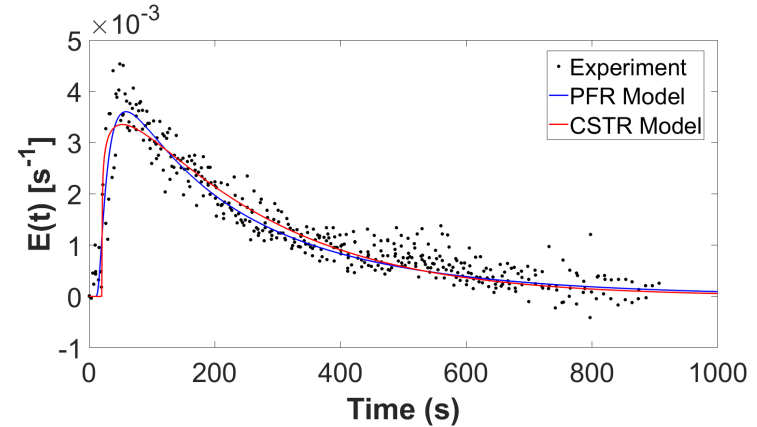


- **Time to Product:** Time it takes for first material impacted by disturbance to reach diversion point
- **Time to Clear:** Time it takes for all material impacted by disturbance to reach diversion point, at which time the process should be back within a state of control

# Residence Time Distribution Models



- RTDs commonly fitted to two models
  - **Axial Dispersion Model**
    - Plug flow reactor (PFR) with back-mixing
    - Peclet number ( $Pe$ ) describes degree of dispersion
    - Best suited for cases of low dispersion
  - **Tanks-in-Series Model**
    - Chain of continuous stirred-tank reactors (CSTRs)
    - Theoretical number of tanks ( $N$ ) describes degree of dispersion
  - Both models also estimate MRT ( $\tau$ ) as a fitting parameter of dimensionless time:
    - $\theta = (t - t_{lag})/\tau$
- A good model fit does not necessarily imply fitting parameters are accurate

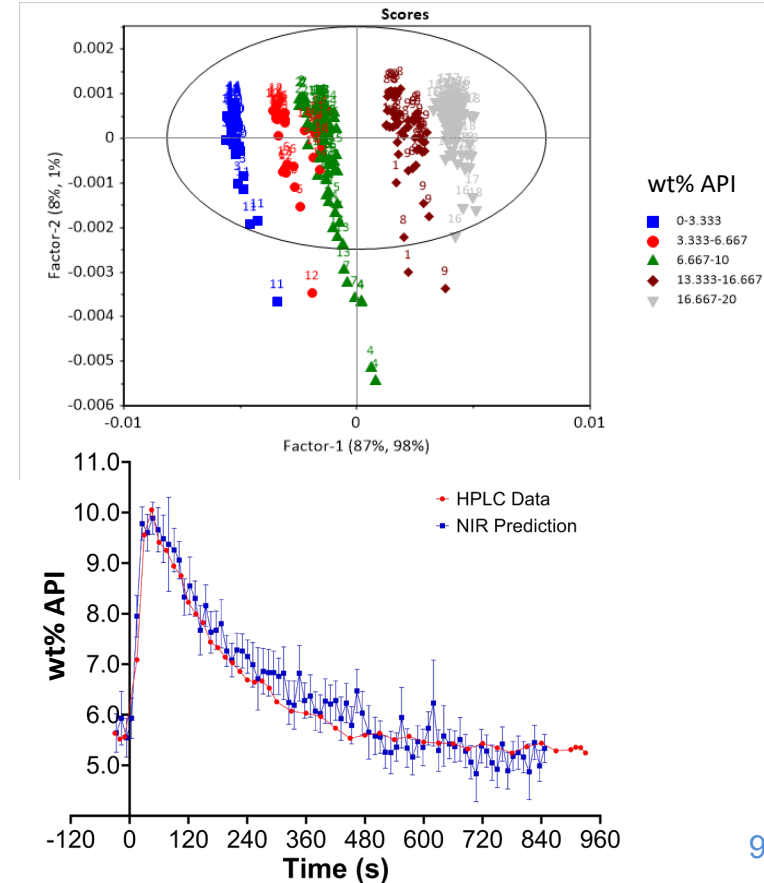


$$\tau E_{PFR}(t) = \begin{cases} 0, & t \leq t_{lag} \\ \sqrt{\frac{Pe}{4\pi\theta}} * \exp\left(-\frac{Pe[1-\theta]^2}{4\theta}\right), & t > t_{lag} \end{cases}$$
$$\tau E_{CSTR}(t) = \begin{cases} 0, & t \leq t_{lag} \\ \theta^{N-1} \frac{N^N}{\Gamma(N)} * \exp[-N\theta], & t > t_{lag} \end{cases}$$



# PAT Data Collection and Model Development

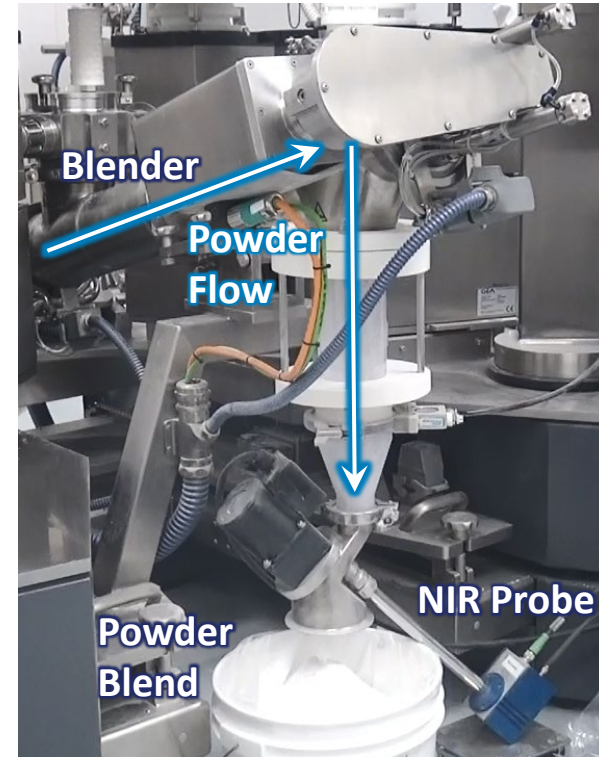
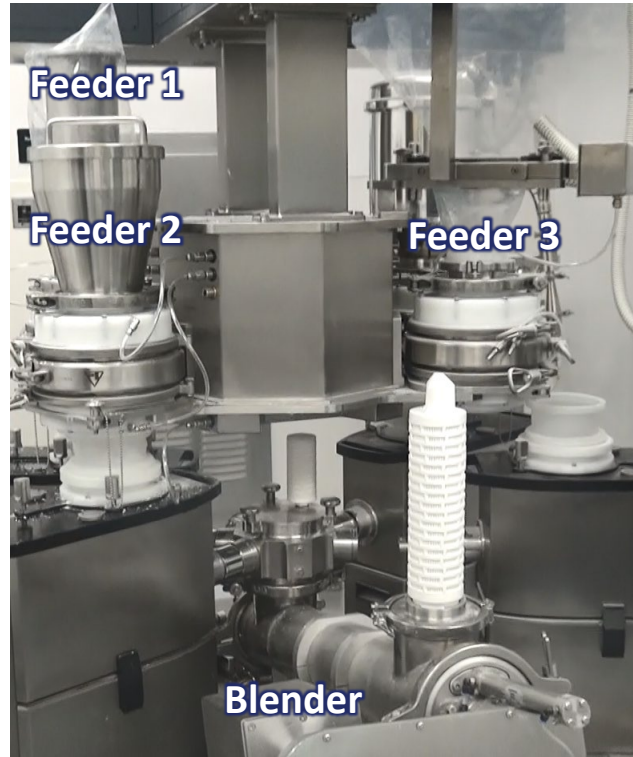
- PAT calibration model(s) established under controlled conditions mimicking the in-line process measurements as closely as possible
  - Capture appropriate component concentration ranges and possible sources of variability (e.g., process, analyzer, material characteristics)
  - Equivalent sample presentation conditions
- Multivariate models may be employed to estimate sample characteristics from spectral variation
  - Model parameter selection (e.g., pretreatments, wavelength range, number of factors) should consider both predictive performance and model robustness
  - External validation with independent samples representative of the commercial process



# Continuous Feeding and Blending Unit



- Three loss-in-weight feeders feed API and excipients into a continuous tubular blender
- Blender contains configurable shaft with 28 elements
  - Either transport or mixing
  - 2 blades per element
- Near infrared (NIR) spectrometer positioned below blender outlet



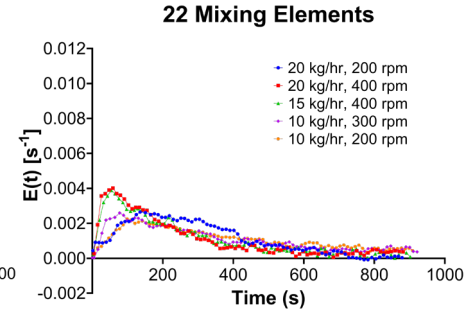
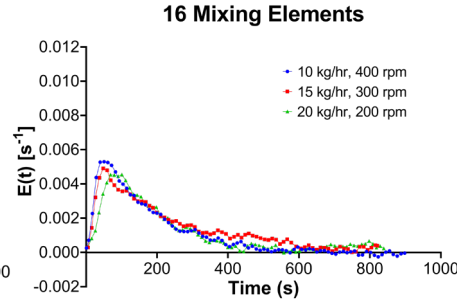
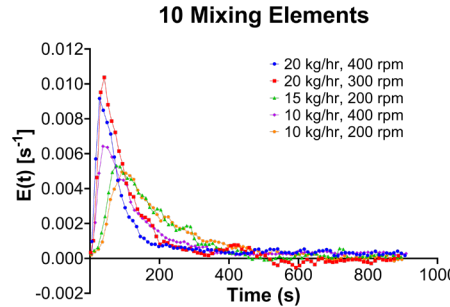
Continuous feeding and blending unit used to perform experiments

# Effect of Process Parameters on RTDs



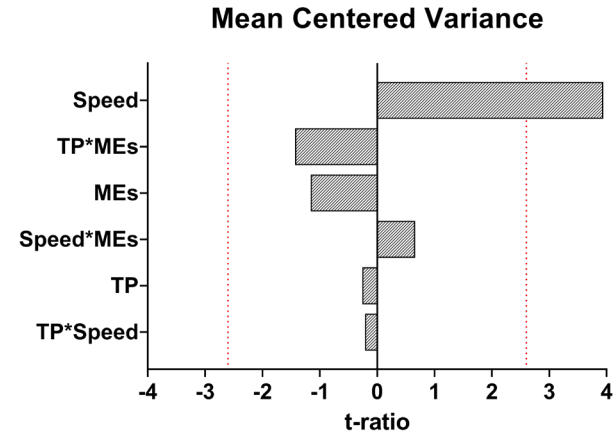
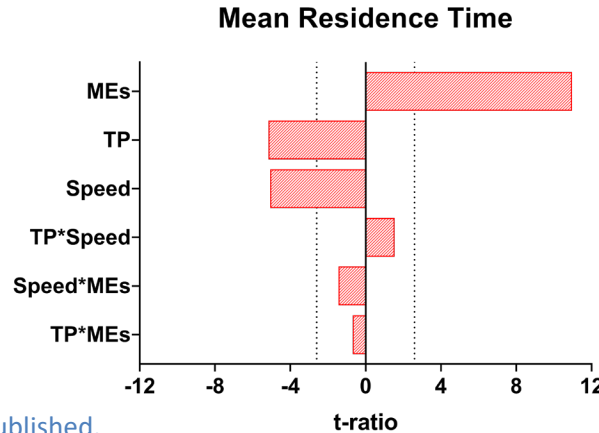
- Mean Residence Time:

- Increased with additional mixing elements (MEs)
- Decreased with increasing total throughput (TP) and blender speed (Speed)



- Mean Centered Variance (i.e., pulse dispersion):

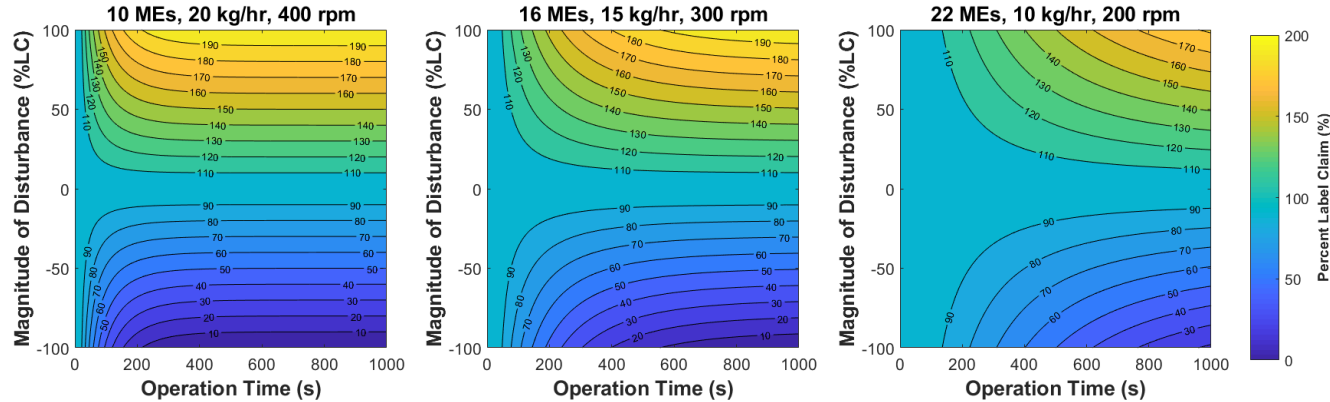
- Increased with increasing blender speed



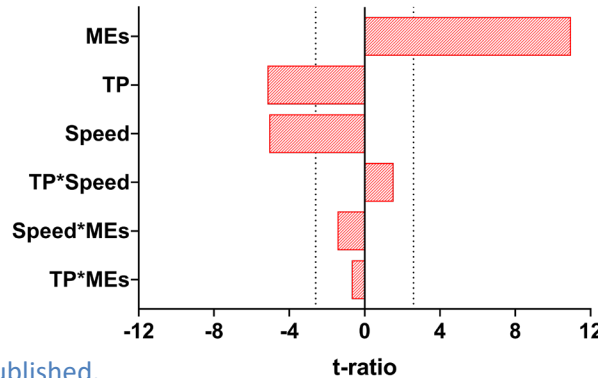
# Effect of Process Parameters on RTDs



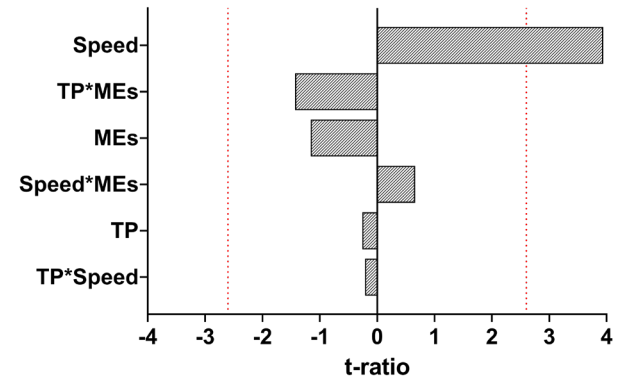
- Mean Residence Time:
  - Increased with additional mixing elements (MEs)
  - Decreased with increasing total throughput (TP) and blender speed (Speed)
- Mean Centered Variance (i.e., pulse dispersion):
  - Increased with increasing blender speed
- Most operating flexibility using settings with high mean residence time



Mean Residence Time



Mean Centered Variance

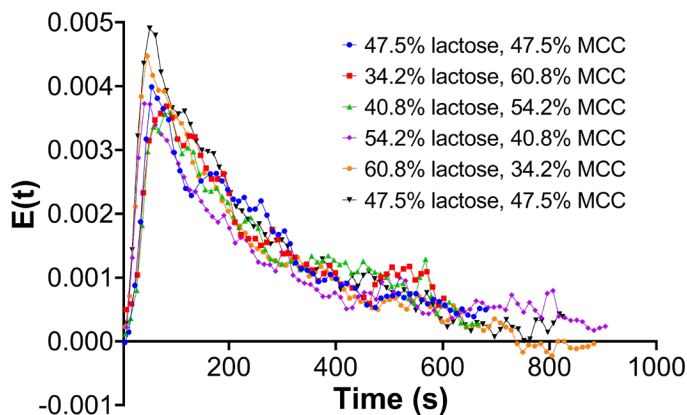


# Effect of Bulk Material Properties on RTDs



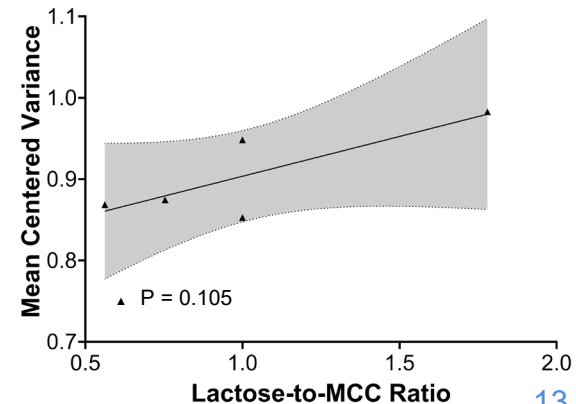
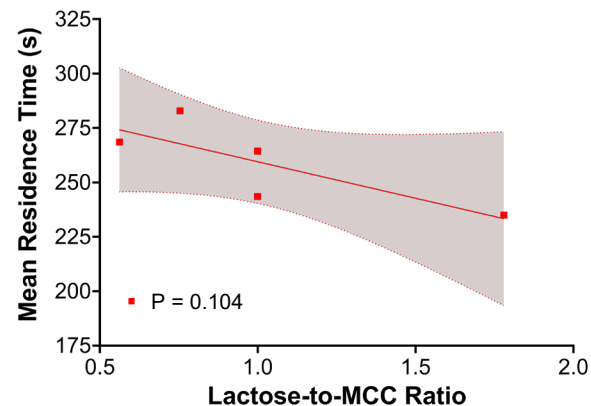
- Varied excipient ratio at fixed process conditions and API flow rate

- Lactose more cohesive with higher bulk density, MCC free flowing with lower bulk density



- Bulk properties should be considered when evaluating RTDs

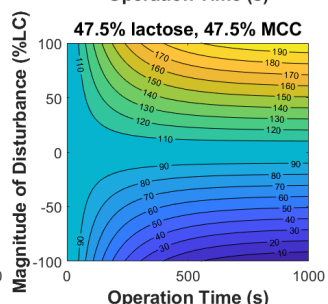
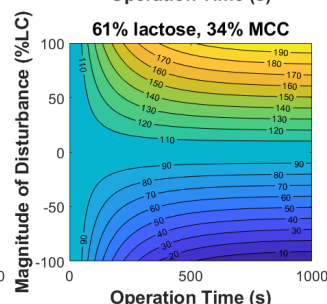
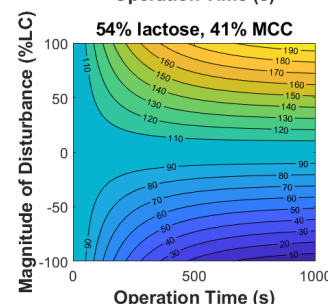
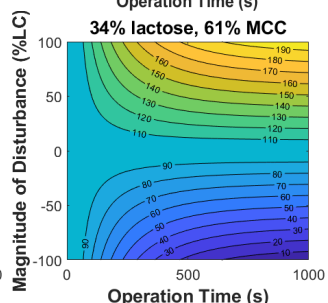
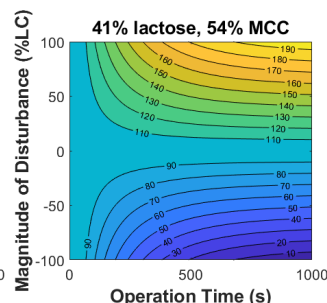
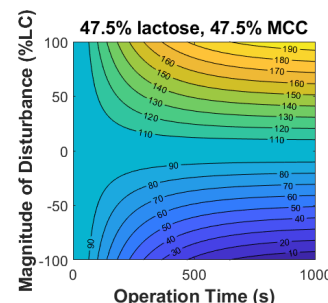
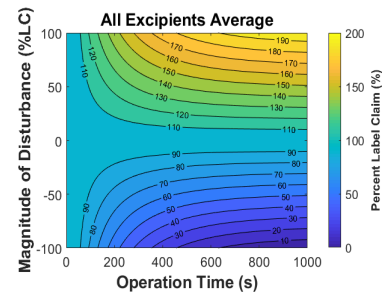
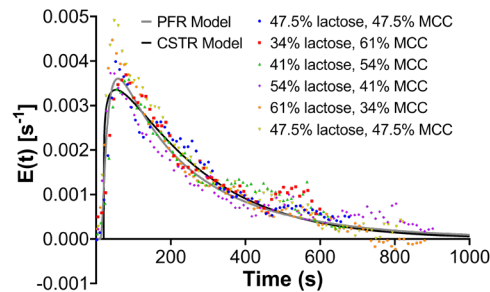
- Increasing lactose-to-MCC ratio (higher bulk density, cohesion) slightly decreased MRT and increased MCV (both  $P \approx 0.10$ )
- Understanding the impact of the shift in MRT and MCV can be demonstrated by evaluating the impact of bulk material properties on dampening disturbances



# Effect of Bulk Material Properties on RTDs



- Is an overall fit encompassing data sets from all blending runs with varying excipient ratio an adequate fit for individual runs?
- Funnel plot of combined data fit similar to funnel plots of individual runs
  - Suggests overall fit may adequately represent RTD across range of excipient ratios
  - Safety buffers can be used to account for residual uncertainty depending on the application



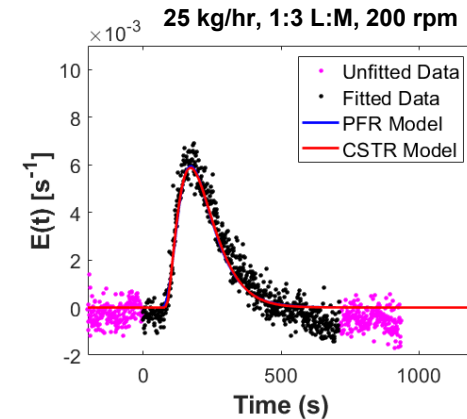
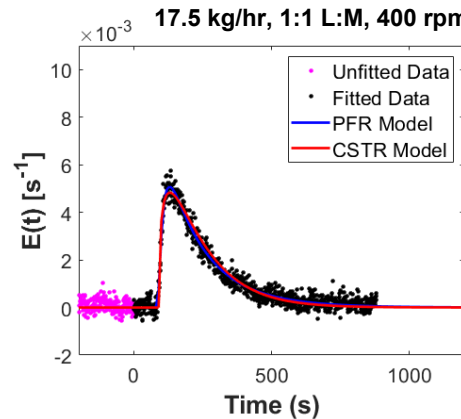
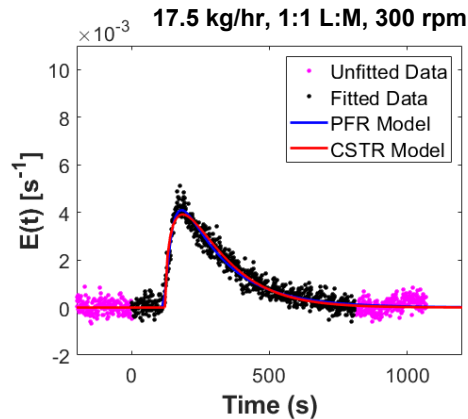
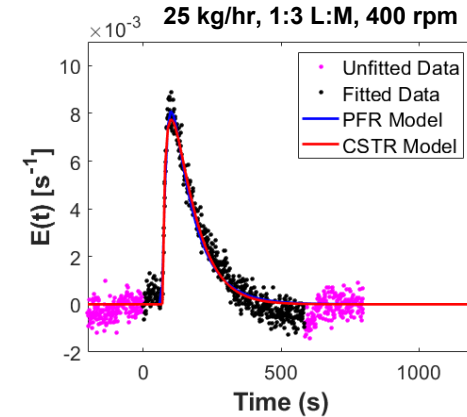
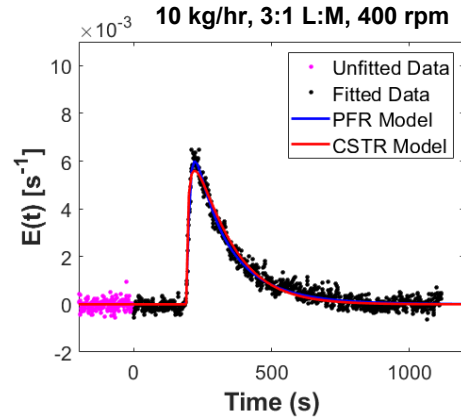
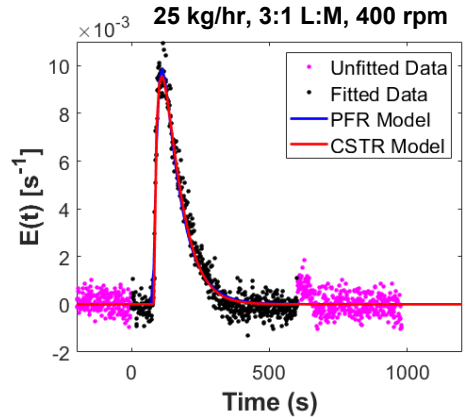


# RTD Model Fitting



- Normalized API tracer concentration curves (RTDs) fitted to **PFR** and **CSTR** models
- Both models exhibited similar goodness of fit

- Data prior to tracer insertion and after API feeder refills (magenta) excluded from model fitting

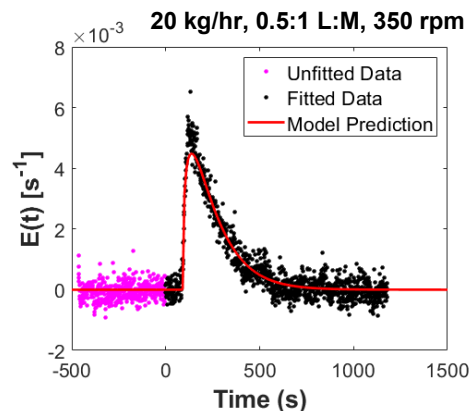
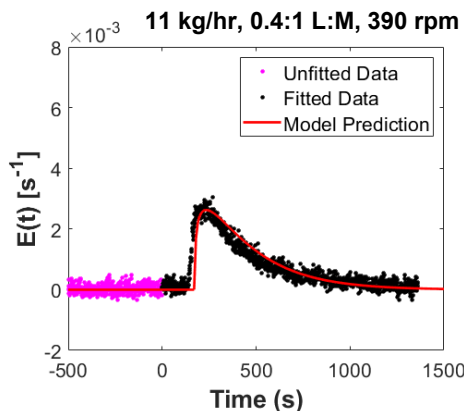
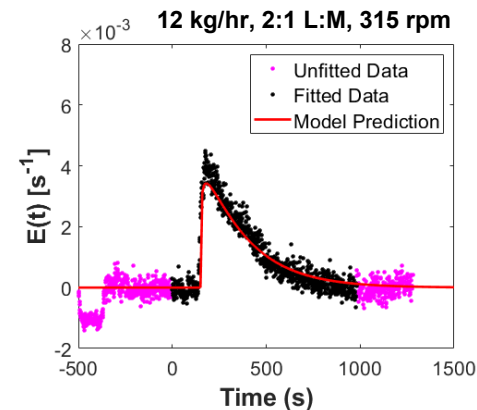
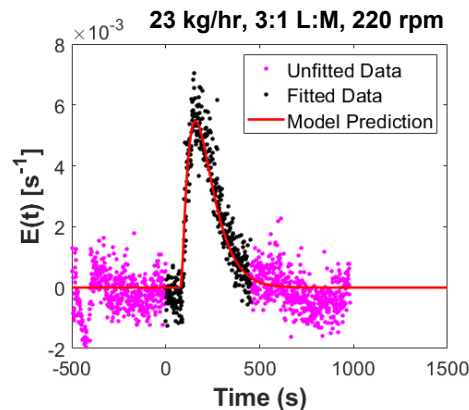
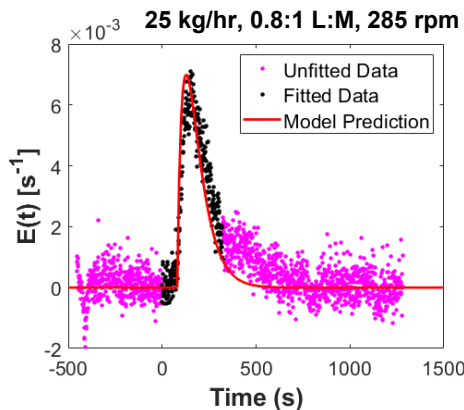


# RTD Model Validation



- **CSTR model** used to predict RTD of external validation blending runs, projected over measured data

- Data prior to tracer insertion and after API feeder refills (magenta) excluded from model fitting





# Concluding Thoughts



- Understanding how bulk material properties and process conditions affect the RTD of a process is critical for process understanding
  - Significant differences in RTDs were observed following changes in process parameters (e.g., blender speed, impeller configuration)
  - Slight differences in RTDs were observed following changes in bulk properties
- RTD models can enable real-time prediction of feeding material disturbances on blend and content uniformity
  - The level of understanding demonstrated should be commensurate with how the RTD models are used as part of the control strategy
  - RTD model assumptions should be justified with appropriate considerations for the limitations of the model



# Acknowledgments

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